

# Development of reliable interaction potential for and results of molecular dynamics simulations of $\text{ZrO}_2$ film growth

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## Acknowledgment

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## Motivation

- Reproducing the film growth by MD allows one to disentangle
  - crystal nucleation and crystal growth
  - effects of individual parts of the total particle flux
  - correlated parameters such as ion energy and temperature



- Relationships between growth conditions and
  - crystal nucleation (non-epitaxial template)
  - crystal growth (epitaxial template)

## Outline

- Development of reliable interaction potential for  $\text{ZrO}_2$   
*[J. Houska, Comp. Mater. Sci. 111 (2016) 209–217]*
- Results of growth simulations of  $\text{ZrO}_2$   
*[J. Houska, Surf. Coat. Technol. 304 (2016) 23–30]*



## Recursive atom-by-atom simulation protocol

- 1) **Substrate or previously nucleated crystal**  
(given structure & temperature)
- 2) **New atoms**  
(given energy distribution function)
- 3) **Fixed-energy (NVE) run**  
(particle collisions and energy dissipation)
- 4) **Fixed-temperature (NVT) run**  
(to reestablish the deposition temperature)
- 5) **Removal** of resputtered/desorbed particles and return to 2

crucial for success of classical MD: reliable potentials  
(force fields) describing interatomic interactions

## Buckingham interaction potential

$$U = Ae^{-r/\rho} - Cr^{-6} + q_1q_2/4\pi\epsilon r$$

- State the art for ionic metal oxides
- Potential parameters in the literature for most materials:

👍 crystal phases of interest constitute energy minima:  
**correct lattice constants and formation energies**

👎 fitted with other simulation protocols in mind



**wrong preferred coordination numbers**



unsuitable for reliable growth simulations



## Literature potentials for $\text{ZrO}_2$ lead to undercoordination

Criterion of success: Zr coordination,  $N_{\text{Zr}}$

Experiment:  $N_{\text{Zr}} = 8$  (c- & t- $\text{ZrO}_2$ )

$N_{\text{Zr}} = 7$  (m- $\text{ZrO}_2$ )

Ab-initio:  $N_{\text{Zr}} \leq 7$  (a- $\text{ZrO}_2$ )

Growth by simulations on amorphous  $\text{ZrO}_2$

Schelling 2001:  $N_{\text{Zr}} < 6$

Dwiwedi 1990+Kilo 2003:  $N_{\text{Zr}} < 5$

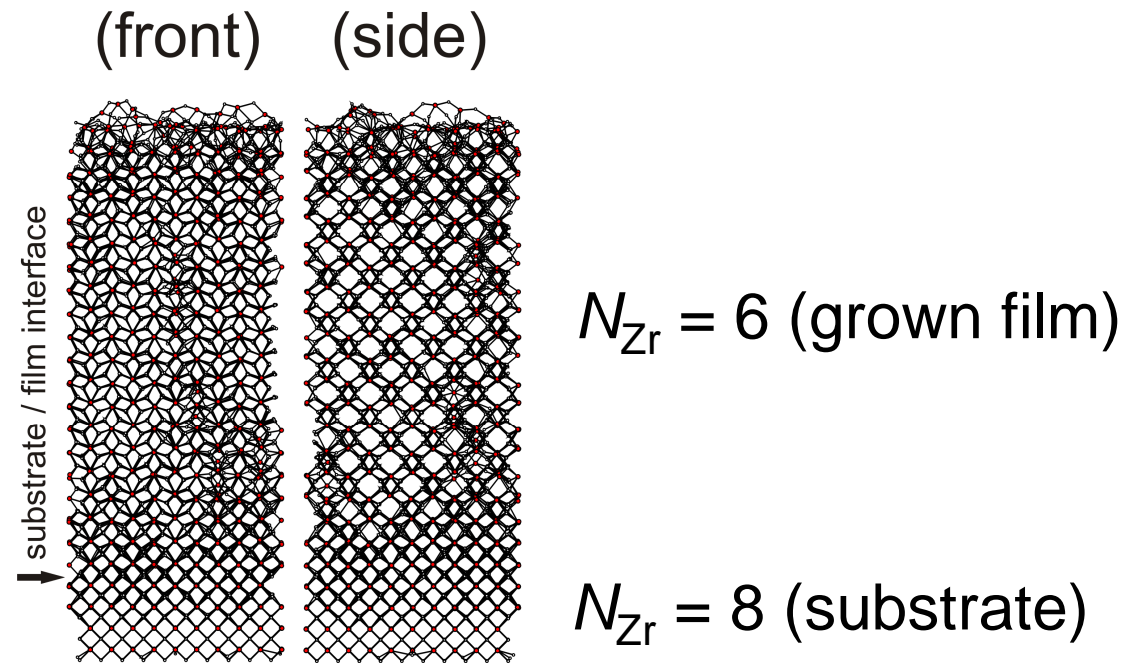
Lewis 1985:  $N_{\text{Zr}} = 0$  (desorption)

Noordhoek 2014 (variable-charge):  $N_{\text{Zr}} < 4$

Growth by simulations on cubic  $\text{ZrO}_2$

Schelling 2001:  $N_{\text{Zr}} = 6$  (fictitious rutile-like structure)

## Literature potentials for $\text{ZrO}_2$ lead to undercoordination



Growth by simulations on cubic  $\text{ZrO}_2$

Schelling 2001:

$N_{\text{Zr}} = 6$  (fictitious rutile-like structure)

## Fitting of reliable $\text{ZrO}_2$ potential

$$U = Ae^{-r/\rho} - Cr^{-6} + q_1q_2/4\pi\epsilon r$$

Starting point:

**full-charge** Schelling pot. ( $A, \rho, C$  at  $q_{\text{Zr}} = +4e, q_{\text{O}} = -2e$ )

👎 incorrect  $N_{\text{Zr}}$

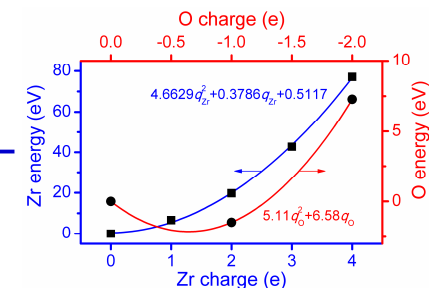
Solution:

**partial-charge** ( $q_{\text{Zr}}$  between 0 and  $+4e$ )

👍 additional degree of freedom  $\Rightarrow$  correct  $N_{\text{Zr}}$

👍 closer to the experiment

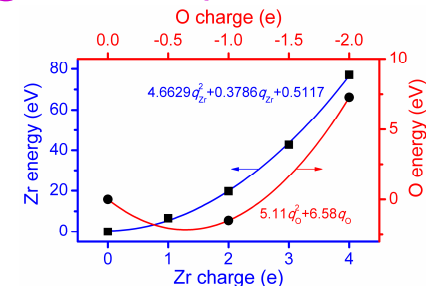
👍 avoiding too high potential energies of ionization



## Fitting of reliable $\text{ZrO}_2$ potential

$$U = Ae^{-r/\rho} - Cr^{-6} + q_1q_2/4\pi\epsilon r$$

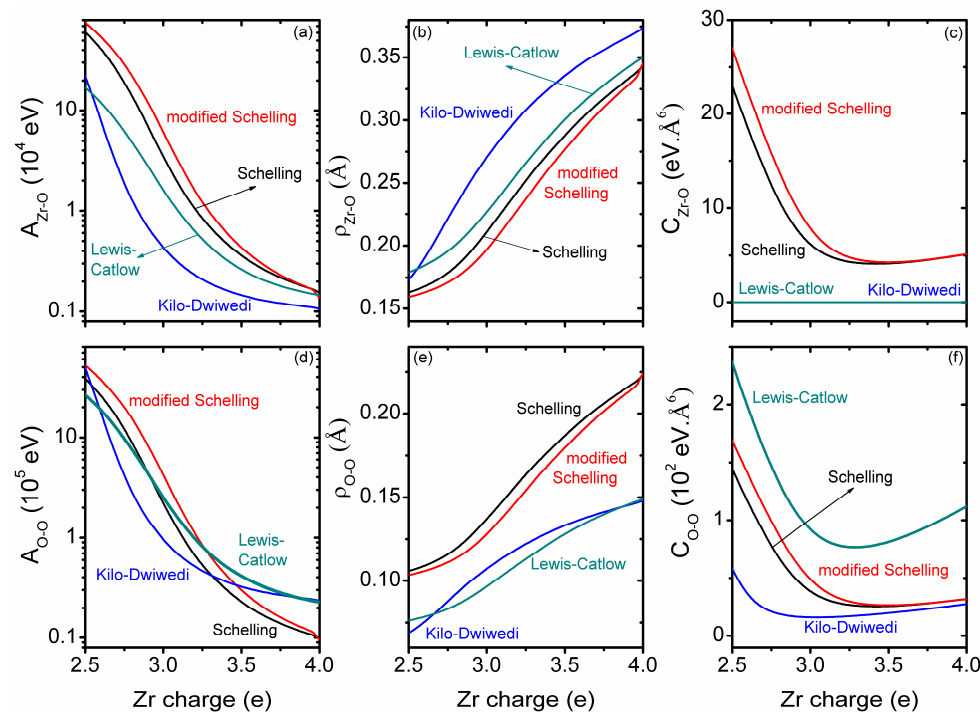
- 1) Starting-point potential - correct lattice const. and energies
- 2)  $q_{\text{Zr}} = q_{\text{Zr}} - \Delta q_{\text{Zr}} \Rightarrow$  new (incorrect) lattice const. and energies
- 3) changing the length scale  
 $\Rightarrow$  new  $A, \rho, C, q_{\text{Zr}}$   
 $\Rightarrow$  correct lattice constants
- 4) changing the energy scale at preserved length scale  
(quadratic dependence of ionization energy on  $q_{\text{Zr}}$ ,  
thus quadratic equation for the rescaling factor)  
 $\Rightarrow$  new  $A, \rho, C, q_{\text{Zr}}$   
 $\Rightarrow$  correct formation energies
- 5) return to 2



## Fitting of reliable $\text{ZrO}_2$ potential

$$U = Ae^{-r/\rho} - Cr^{-6} + q_1q_2/4\pi\epsilon r$$

Results :  $q_{\text{Zr}}$ -dependent short-range parameters  $A$ ,  $\rho$ ,  $C$   
(shown for various starting-point potentials, one is used below)

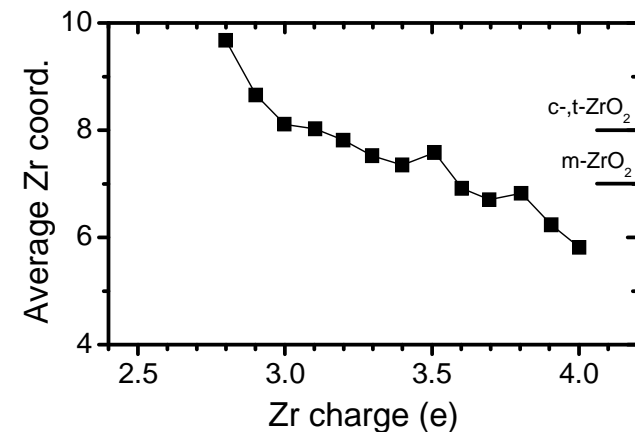
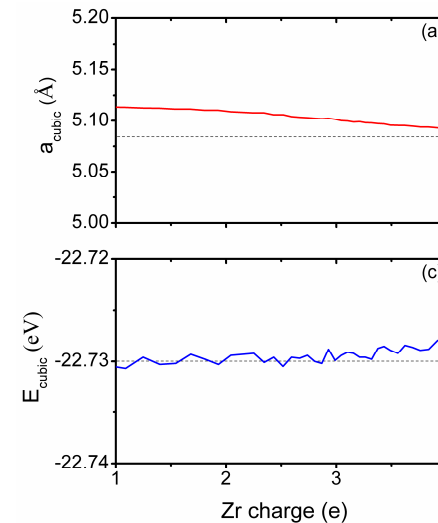


## Fitting of reliable $\text{ZrO}_2$ potential

Newly fitted partial-charge potentials lead to

the same lattice constants and energies  
(fitted for c- & t- $\text{ZrO}_2$ , shown for c- $\text{ZrO}_2$ )

different coordination numbers  
obtained by growth on a- $\text{ZrO}_2$



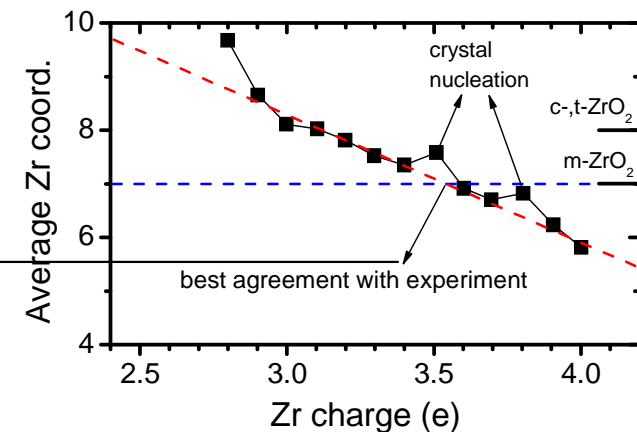
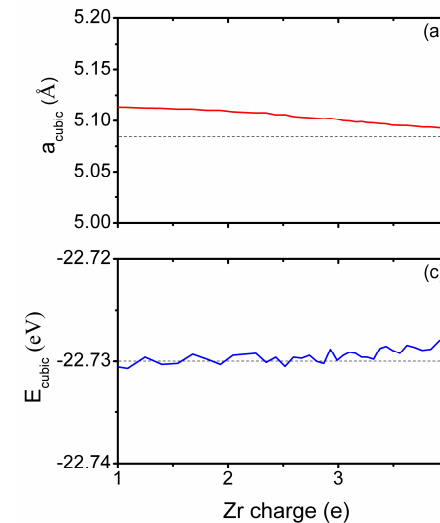
## Fitting of reliable $\text{ZrO}_2$ potential

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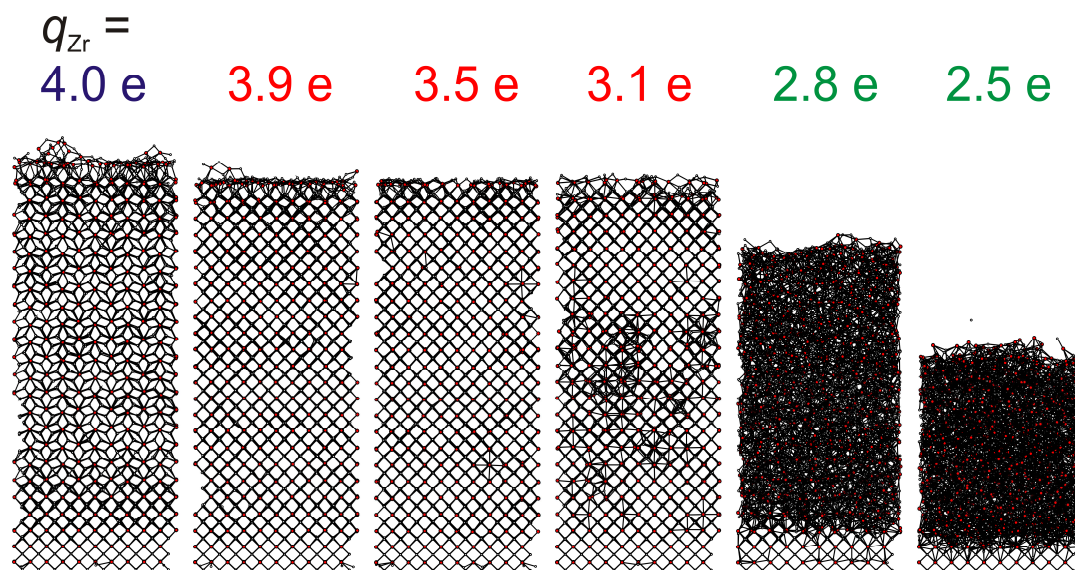
different coordination numbers  
obtained by growth on a- $\text{ZrO}_2$

experimental  $N_{\text{Zr}}$  for  $q_{\text{Zr}} = 3.542$



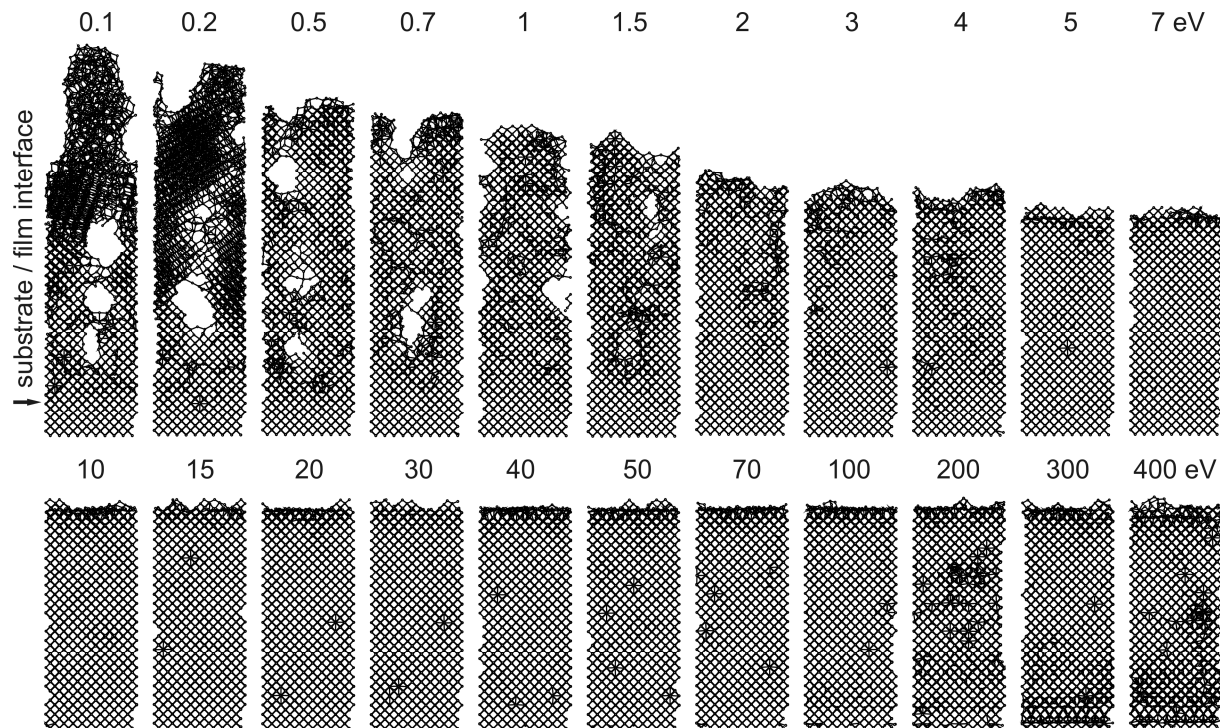
## Test of fitted $\text{ZrO}_2$ potentials

- Growth on a- $\text{ZrO}_2$ : experimental  $N_{\text{Zr}}$  for  $q_{\text{Zr}} = 3.542$
- Growth on c- $\text{ZrO}_2$  (under optimum growth conditions):
  - $q_{\text{Zr}} = 4.0$  : undercoordination, fictitious rutile-like
  - $q_{\text{Zr}}$  around 3.5 : indeed, c- $\text{ZrO}_2$  growth
  - $q_{\text{Zr}}$  too low : overcoordination, amorphization



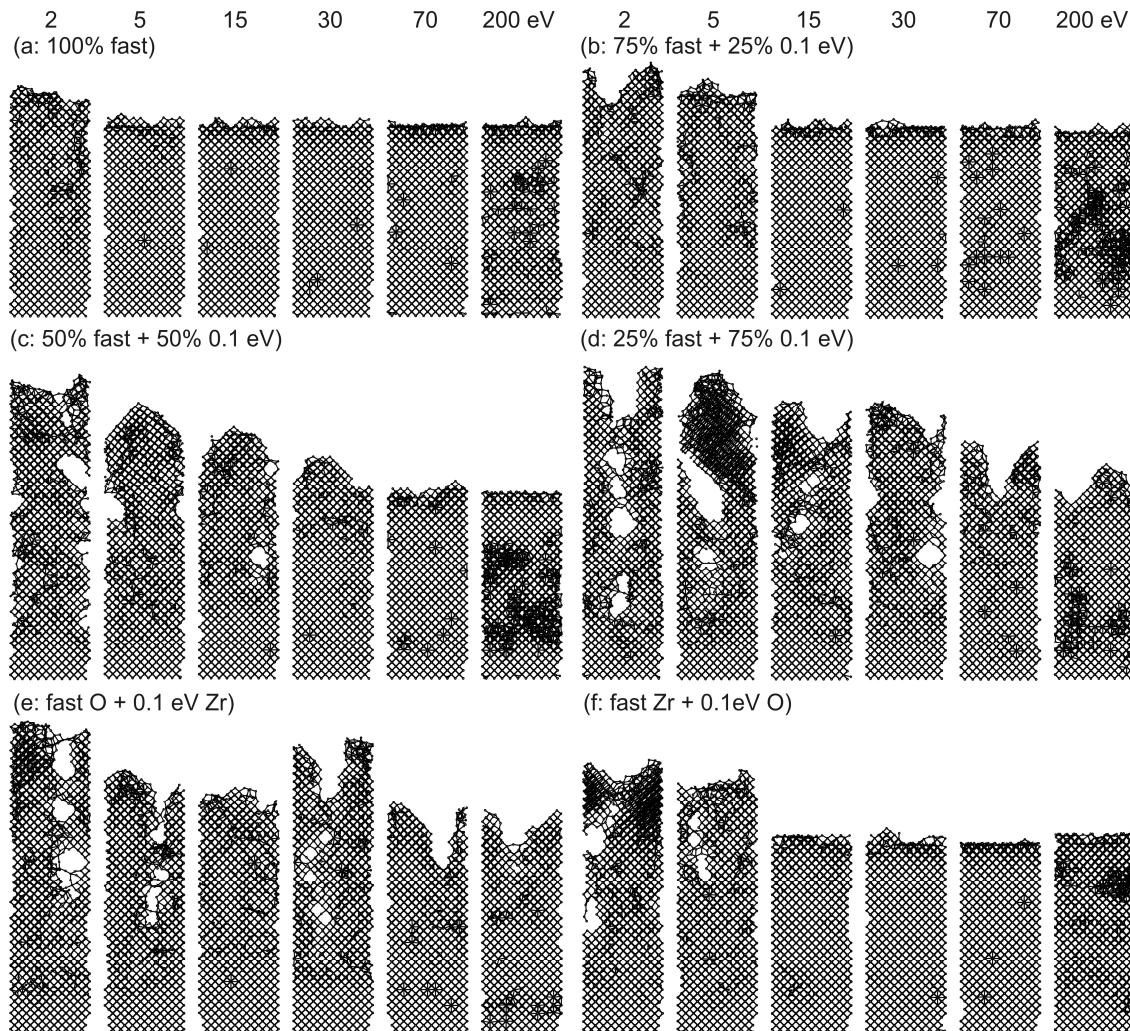


## c-ZrO<sub>2</sub> growth - effect of energy, $E$



- Densification with increasing energy
- Same energy of all atoms  $\Rightarrow$  fully densified at  $E \geq 5$  eV
- Defects at  $E > 100$  eV

## c-ZrO<sub>2</sub> growth - effect of energy distribution function



- Increasing fraction of slow atoms  $\Rightarrow$  less densified

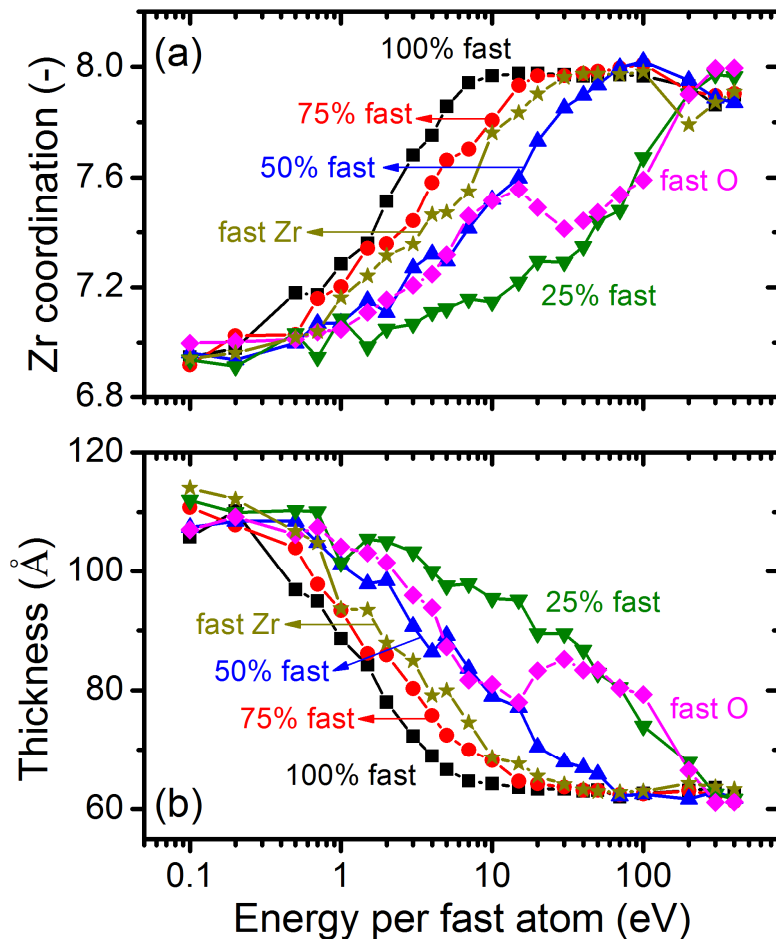
- Fast heavy Zr (33% of all atoms): densification

×

- Fast light O (66% of all atoms): poor densification

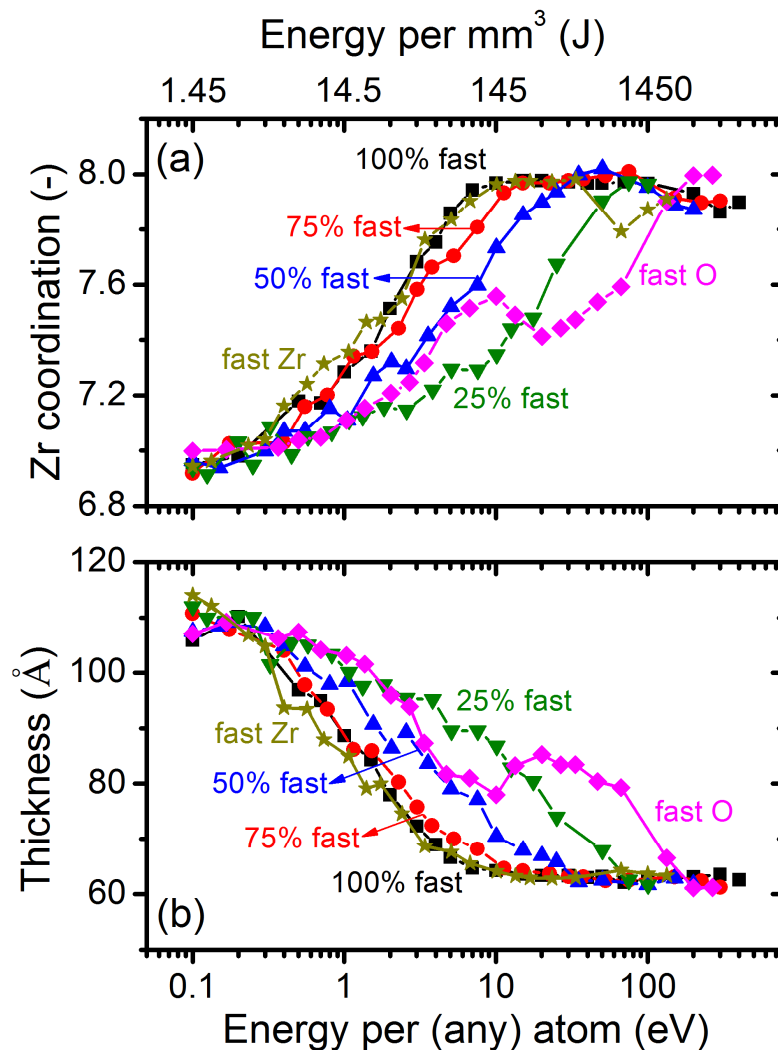
## c-ZrO<sub>2</sub> growth - effect of energy distribution function

(quantification of the above results)



- Increasing fraction of slow atoms  $\Rightarrow$  less densified (low  $N_{\text{Zr}}$ , high thickness)
- Fast heavy Zr: densification
- × Fast light O: poor densification
- Reproducible local  $N_{\text{Zr}}$  minima (limit for inducing specific kind of defect)

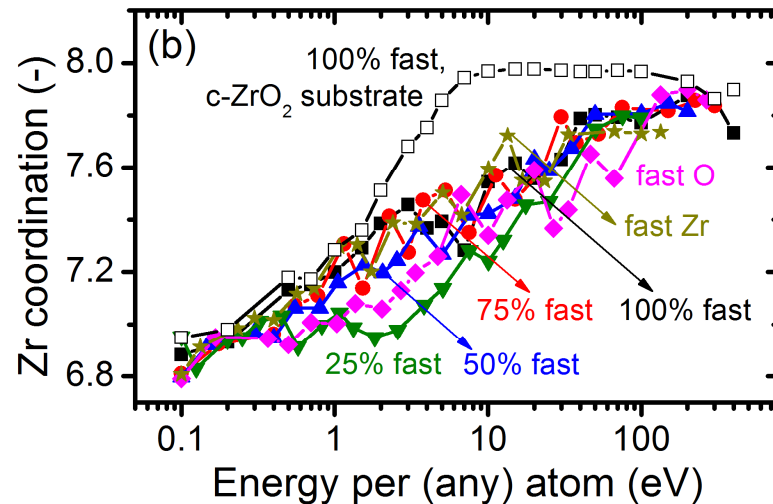
## c-ZrO<sub>2</sub> growth - effect of energy distribution function



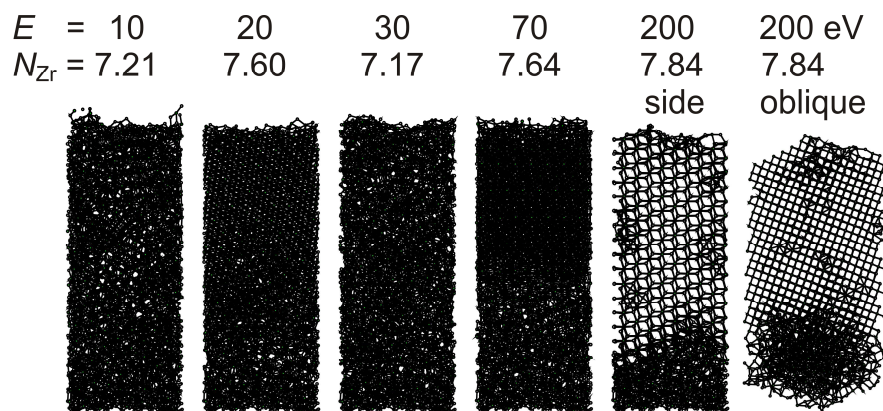
The same data as a function of energy **per any atom** (not per fast atom)

- Dependencies still do not overlap
- ↓
- Presence of slow atoms cannot be compensated by higher energy of fast atoms (ions) - correct average energy is not enough for crystal growth

## Amorphous $\text{ZrO}_2$ growth and c- $\text{ZrO}_2$ nucleation

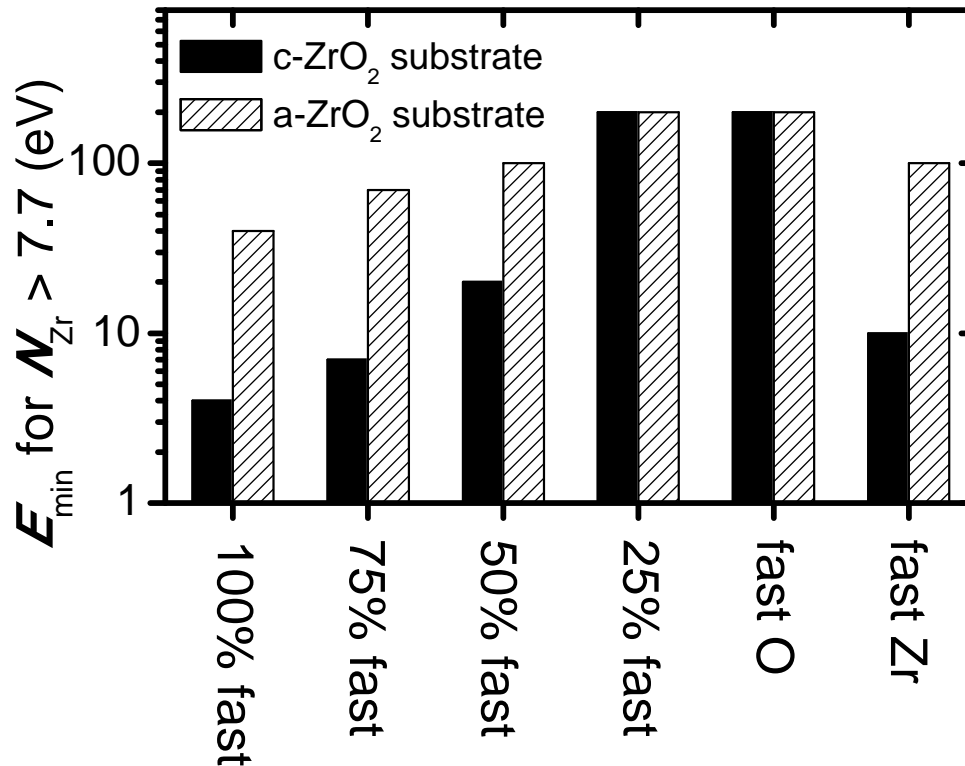


- Dependencies closer to each other  
 ↓
- Correct average energy is not enough for crystal growth, but  $\pm$  enough for densification of amorphous
- Frequent c- $\text{ZrO}_2$  nucleation at energy of fast atoms (for various energy distribution functions)  $\geq 200$  eV





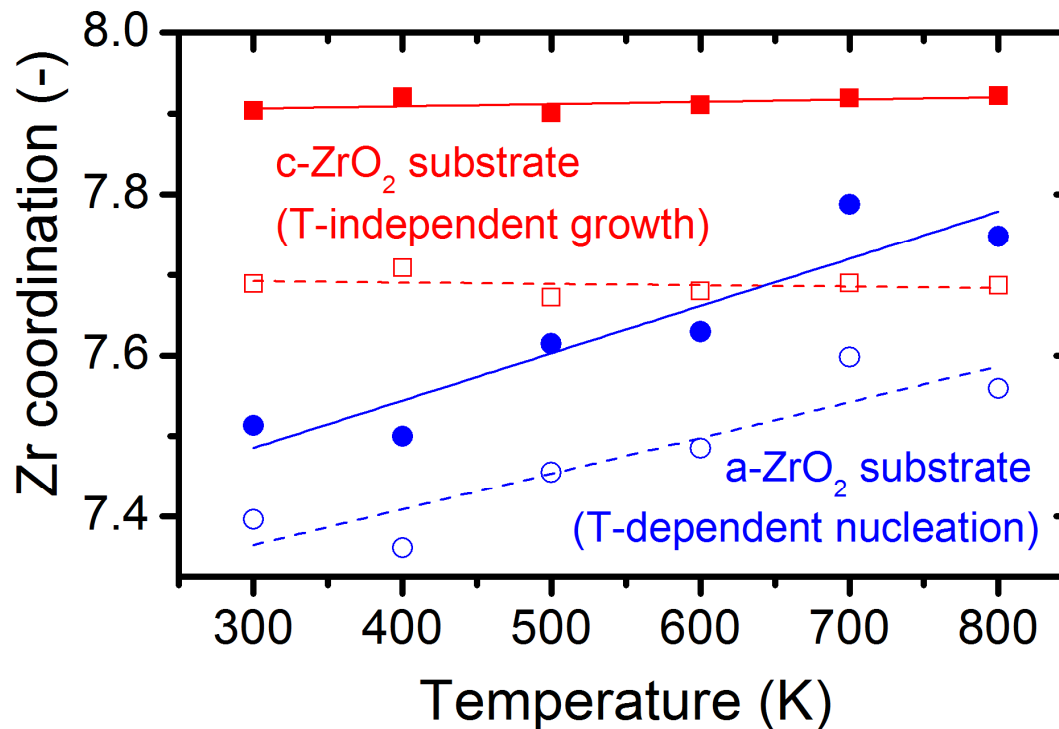
## Growth × nucleation: effect of energy and EDF



minimum energy of fast atoms  
leading to crystallinity &  
densification ( $N_{\text{Zr}} > 7.7$ )

- Epitaxial growth can be utilized at optimum EDF only:  
then, **5 eV** of all atoms is enough for dense crystal growth
- Non-optimum EDF or amorphous substrate:  
**200 eV** of some atoms is needed for frequent (re)nucleation

## Growth × nucleation: effect of temperature



full symbols:  
average over 3.0 - 400 eV  
empty symbols:  
average over 0.1 - 400 eV

- Growth of existing crystals is almost T-independent
- Nucleation of crystals (on amorphous substrate) takes place on longer time scale, is T-dependent

## Conclusions

- Procedure for improvement (coorrect coordination numbers!) of literature interaction potentials  $\Rightarrow$  reliable  $\text{ZrO}_2$  potential
- Crystal growth (5 eV limit at optimum EDF)
- Crystal nucleation (200 eV limit)
- EDF-dependent & mass/momentum-dependent growth
- T-independent growth  $\times$  T-dependent nucleation



Force field for realistic molecular dynamics simulations of  $\text{ZrO}_2$  growth  
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Molecular dynamics study of the growth of crystalline  $\text{ZrO}_2$   
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