

OPERACE VEKTOROVÉ ANALÝZY

| Název Symbol | Soustava kartézských souřadnic x, y, z | Soustava válcových (cylindrických) souřadnic r, α, z | Soustava kulových souřadnic r, α, ϑ r má jiný význam než v cylindrickém systému. |
|--|---|--|--|
| vektor \mathbf{a} | $\mathbf{a} = i a_x + j a_y + k a_z$ $\mathbf{a} = (a_x, a_y, a_z)$ | $\mathbf{a} = r_0 a_r + \alpha_0 a_\alpha + k a_z$ $\mathbf{a} = (a_r, a_\alpha, a_z)$ | $\mathbf{a} = r_0 a_r + \alpha_0 a_\alpha + \vartheta_0 a_\vartheta$ $\mathbf{a} = (a_r, a_\alpha, a_\vartheta)$ |
| Hamiltonův operátor ∇ | $i \frac{\partial}{\partial x} + j \frac{\partial}{\partial y} + k \frac{\partial}{\partial z}$ | $r_0 \frac{\partial}{\partial r} + \alpha_0 \frac{1}{r} \frac{\partial}{\partial \alpha} + k \frac{\partial}{\partial z}$ | $r_0 \frac{\partial}{\partial r} + \alpha_0 \frac{1}{r \sin \vartheta} \frac{\partial}{\partial \alpha} + \vartheta_0 \frac{1}{r} \frac{\partial}{\partial \vartheta}$ |
| grad $\varphi = \nabla \varphi$ | $i \frac{\partial \varphi}{\partial x} + j \frac{\partial \varphi}{\partial y} + k \frac{\partial \varphi}{\partial z}$ | $r_0 \frac{\partial \varphi}{\partial r} + \alpha_0 \frac{1}{r} \frac{\partial \varphi}{\partial \alpha} + k \frac{\partial \varphi}{\partial z}$ | $r_0 \frac{\partial \varphi}{\partial r} + \alpha_0 \frac{1}{r \sin \vartheta} \frac{\partial \varphi}{\partial \alpha} + \vartheta_0 \frac{1}{r} \frac{\partial \varphi}{\partial \vartheta}$ |
| div $\mathbf{a} = \nabla \cdot \mathbf{a}$ | $\frac{\partial a_x}{\partial x} + \frac{\partial a_y}{\partial y} + \frac{\partial a_z}{\partial z}$ | $\frac{\partial}{\partial r} (r a_r) + \frac{1}{r} \frac{\partial a_\alpha}{\partial \alpha} + \frac{\partial a_z}{\partial z}$ | $\frac{1}{r^2} \frac{\partial (r^2 a_r)}{\partial r} + \frac{1}{r \sin \vartheta} \left[\frac{\partial}{\partial \vartheta} (a_\vartheta \sin \vartheta) + \frac{\partial a_\alpha}{\partial \alpha} \right]$ |
| rot $\mathbf{a} = \nabla \times \mathbf{a}$ | $\text{rot}_x \mathbf{a} = \frac{\partial a_z}{\partial y} - \frac{\partial a_y}{\partial z}$ $\text{rot}_y \mathbf{a} = \frac{\partial a_x}{\partial z} - \frac{\partial a_z}{\partial x}$ $\text{rot}_z \mathbf{a} = \frac{\partial a_y}{\partial x} - \frac{\partial a_x}{\partial y}$ | $\text{rot}_r \mathbf{a} = \frac{1}{r} \frac{\partial a_z}{\partial \alpha} - \frac{\partial a_\alpha}{\partial z}$ $\text{rot}_\alpha \mathbf{a} = \frac{\partial a_r}{\partial z} - \frac{\partial a_z}{\partial r}$ $\text{rot}_z \mathbf{a} = \frac{1}{r} \frac{\partial (r a_\alpha)}{\partial r} - \frac{1}{r} \frac{\partial a_r}{\partial \alpha}$ | $\text{rot}_r \mathbf{a} = \frac{1}{r \sin \vartheta} \left[\frac{\partial}{\partial \vartheta} (a_\alpha \sin \vartheta) - \frac{\partial a_\vartheta}{\partial \alpha} \right]$ $\text{rot}_\alpha \mathbf{a} = \frac{1}{r} \frac{\partial}{\partial r} (r a_\vartheta) - \frac{1}{r} \frac{\partial a_r}{\partial \vartheta}$ $\text{rot}_\vartheta \mathbf{a} = \frac{1}{r \sin \vartheta} \frac{\partial a_r}{\partial \alpha} - \frac{1}{r} \frac{\partial}{\partial r} (r a_\alpha)$ |
| Laplaceův operátor | $\Delta \varphi = \frac{\partial^2 \varphi}{\partial x^2} + \frac{\partial^2 \varphi}{\partial y^2} + \frac{\partial^2 \varphi}{\partial z^2}$ | $\Delta \varphi = \frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial \varphi}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2 \varphi}{\partial \alpha^2} + \frac{\partial^2 \varphi}{\partial z^2}$ | $\Delta \varphi = \frac{1}{r^2} \left[\frac{\partial}{\partial r} \left(r^2 \frac{\partial \varphi}{\partial r} \right) + \frac{1}{\sin \vartheta} \frac{\partial}{\partial \vartheta} \left(\sin \vartheta \frac{\partial \varphi}{\partial \vartheta} \right) + \frac{1}{\sin^2 \vartheta} \frac{\partial^2 \varphi}{\partial \alpha^2} \right]$ |
| Dif. rovnice vektor. čar pole \mathbf{a} | $\frac{dx}{a_x} = \frac{dy}{a_y} = \frac{dz}{a_z}$ | $\frac{dr}{a_r} = \frac{r d\alpha}{a_\alpha} = \frac{dz}{a_z}$ | $\frac{dr}{a_r} = \frac{r d\vartheta}{a_\vartheta} = \frac{r \sin \vartheta d\alpha}{a_\alpha}$ |