1. Introduction

This work deals with modeling and simulation of PV system which can be connected to the distribution power network. It means photovoltaic array. I try to draw up a specification of PV array problems because these sources have certain specific features, that are given by their characters. I give attention to the characteristics of PV cells that influence the reliability and quality of the power supply. I also deal with these behaviour of PV array in the distribution grid, their possible influence on a voltage regulation, influence of their power variation on voltage waveform at the point of connection and also an examination of different variants of PV array connection.

Key words:

Microgrids, renewable energy, renewable power sources, optimalization, PV cell, mathematical model of PV cell, Swing

2. Mathematical model of PV cell

We can substitute PV cell by equivalent electric circuit where is included a power supply and a diode. The power supply produce the current $I_{ph}$ which depends on impinging radiation. Through diode flows the current $I_D$. The current $I$ which flows to load is difference between $I_{ph}$ and $I_D$ and it is reduced by the resistance $R_S$ which represents resistance of cell and connection among cells.

If we connect a resistive load $R$ to cell then working point of cell will be on crossing point voltampere characteristic of cell and load characteristic. Voltampere characteristic of load is a straight line with slope $1/R$. If value of $R$ is too low, the working point is in area between $M$ and $N$ where cell behaves like constant current source. It is more or less short circuit current. But if value of $R$ is high, the working point is in area between $P$ and $S$ where cell behaves like constant voltage source. It means about a open circuit voltage.

Connection with optimal resistance $R_{opt}$ means that PV cell generates maximum output power which is given to product of voltage $U_m$ and current $I_m$. Working point where is the maximum of power and efficiency is in the flexion of voltampere characteristic.

In Fig 3, an voltampere characteristic of a PV cell for only a certain ambient irradiation $G_a$ and only a certain cell temperature $T_c$ is illustrated. The influence of the ambient irradiation $G_a$ and the cell temperature $T_c$ on the cell characteristics in presented in Fig 4.

Fig 3 shows that the open circuit voltage increases logarithmically with the ambient irradiation while the short circuit current is a linear function of the ambient irradiation. The arrow shows in which sense the irradiation and the cell temperature, respectively, increase. The influence of the cell temperature on the voltampere characteristics is illustrated in Fig 4. The dominant effect with increasing cell’s temperature is the linear decrease of the open circuit voltage, the cell being thus less efficient. The short circuit current slightly increases with cell temperature.
Fig 3: Influence of the ambient irradiation on the cell characteristics

Fig 4: Influence of the cell temperature on the cell characteristics

For practical use, PV cells can be electrical connected in different ways: series or parallel. Fig 5 and Fig 6 present how the voltampere curve is modified in the cases when two identical cells are connected in series and in parallel.

It is seen that voltampere characteristics of series interconnected cells can be found by adding, for each current, the different voltages of the individual cells. On the other hand, for parallel cells the currents of the individual cells must be added at each voltage in order to find the overall voltampere curve.

3. Parameters of PV cell for normal specification

standard conditions:
- Impinging radiation $G_{a,0} = 1000 \text{ W/m}^2$
- Temperature of cell $t_{c,0} = 22 \degree \text{C}$

a) short circuit current $I_{SC,0}$ - the maximum current generated by cell with short-circuited output, ($U_{C} = 0$).

b) open circuit voltage $U_{OC,0}$ - the maximum voltage of cell with disconnected output ($I_{C} = 0$).

c) maximum power $P_{m,0}$ - maximum power of cell, $P_{m,0} = U_{m} \cdot I_{m}$ [W]

From these parameters we can assign so called the Fill Factor: $\text{FF} = \frac{U_{m} \cdot I_{m}}{I_{SC} \cdot U_{OC}} [-]$

The Fill Factor for good cells would be higher than 0.7.

All parameters are valid only for standard condition. If impinging radiation $G_{a}$ or temperature of cell $t_{c}$ change, then open circuit voltage, short circuit current and flexion of voltampere characteristic change as well.

Parameter change of PV cell by influence of change $G$ and $t_{c}$

1) Influence of $G$

Fig 7. Influence of radiation change $G [(\text{W/m}^2) \times 0.1]$ on current and voltage of PV cell.

Open circuit voltage go up logarithmic when impinging radiation go up but short circuit current go up linearly.
2) Influence of temperature change $t_c$ [°C] on current and voltage of PV cell

![Influence of temperature change on current and voltage of PV cell](image)

Fig 8. Influence of temperature change $t_c$ [°C] on current and voltage of PV cell.

When temperature of PV cell go up then open circuit voltage go down linearly and short circuit current go up.

4. Equation describing a behavior of PV cell

a) Equation for computation of PV cell current $I^C$ depending on impress voltage $U^C$.

(it describes waveform of voltampere characteristic):

$$I^C = I^C_{sc} \left[ 1 - \exp \left( U^C - U^C_{oc} / U^C_{m} \right) \right]$$  [A]

b) Computation of short circuit current depending on impinging radiation $G^a$ and temperature of cell $T^C$:

$$I^C_{sc} = C_1 * G^a + k1 * \left( T^C - T^C_0 \right)$$  [A]

$$T^C_0 = 273,15 + T^C_0 = 295,15 \text{ [K]}$$

c) Computation of open circuit voltage depending on impinging radiation $G^a$ and temperature of cell $T^C$:

$$U^C_{oc} = U^C_{sc,0} + C_3 * \left( T^C - T^C_0 \right) - \exp \left( \frac{G^a - G^a_0}{K3} \right) / K4$$  [V]

d) Computation of cell temperature depending on ambient temperature and impinging radiation $G^a$:

$$T^C = t^C_o + 273,15 + C_2 * G^a$$  [K]

Impinging radiation $G^a$ gives a rise to a heating effect of PV cell.

e) Computation of so called the thermal voltage depending on temperature of cell:

$$U^C_t = k * T^C / e$$  [V]

Constant $k = 1,381 * 10^{-23}$ [J/K] is Boltzmann’s constant.

Constant $e = 1,602 * 10^{-19}$ [C] is elementary electric charge.

Constants $C_1, C_2, C_3, K_3, K_4$ are different for different materials. It depends on cells.

5. Real 20 kWp PV system

On the roof of building of Faculty of Electroengineering in Pilsen is installed 20 kWp PV system which is connected to public grid.

The PV system consist of 192 dark blue monocrystalline silicon solar cell modules which are produced by company Isofoton. The specific color of cells was chosen because of the best efficiency of these cells in the time when the system was installed. There are used 8 single-phase DC/AC converters of SunProfi SP 2500. Power consumption of the inverters is covered by solar system itself and the output is symmetrically phased to building’s supply grid on 230V/400V. The connection to building grid is directly through switchboard. Own block transformer is not used because of lowering purchase costs. The array is mounted on building roof, situated outbound and inclined in 45° angle. The fixed inclination is compromise for full year operation and low purchase costs.

Parametres of cell [www.isofoton.com]:

Measurement conditions:
- radiation: 1000 W/m²
- temperature: 25°C

Physical:
- Area of cell: 104,4 cm² (cells 103)
- Large SolarModules I-110 (24V)
- dimension: 1310 x 654 x 39,5
- weight (kg): 11,5
- Number of cells in serie: 72
- Number od cells in parallel: 1
- NOTC (°C): 47
- Type of cell: Monocrystalline Silicon 103 x 103

Electrical:
- Nominal voltage (V): 24
- Maximum power (Wp± 10 %): 110
- Short circuit current (A): 3,38
- Open circuit voltage (V): 43,2
- Maximum power current (A): 3,16
- Maximum power voltage (V): 34,8

Whole PV system consists 8 the same parts with the same power output. Only one of them has components for measurement and monitoring. For good data evaluation of PV array outputs are measured some values like irradiation on horizontal plane, generator array plane irradiation, ambient temperature in the shade, reference sensor temperature, generator cell temperature, generator voltage, generator current, generator power and inverter AC power out. All these parameters are written down to computer file txt every 10 minutes. We can see in this file also maximum and minimum of all these values for 10 minute time period. Then we can analyse measured values and we can compare these parameters with math model of PV array.

These presented measurements were made while almost ideal operation conditions for photovoltaic system. That means constant and high level of solar irradiance and good weather conditions.
6. Model of PV array

Fig. 9. Block math model of PV array in computer program Swing - Controlix

Fig. 10. Screen of running computer program Swing for PV array
5. Conclusion

Solar cells in PV array work only in part of voltampere characteristic near working point where is maximum voltage and maximum current. We assume that photovoltaic system works most of time with maximum efficiency. It means that for modeling of PV cell we should use constants for specific kind of cell near working point.

References

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